

2017 RELEASED FREE RESPONSE SOLUTIONS – MR. CALCULUS

2017 AB #2
(calculator)

There are 50 pounds of bananas on display when the store opens ($t = 0$).

Customers remove bananas from the display at a rate of $f(t) \frac{\text{pounds}}{\text{hr}}$ for $0 < t \leq 12$.

Employees add bananas to the display at a rate of $g(t) \frac{\text{pounds}}{\text{hr}}$ for $3 < t \leq 12$.

(a)

$\int_0^2 f(t) dt \approx 20.05117518$ pounds or 20.051 pounds are removed during the first 2 hours.

(b)

$f'(7) \approx -8.119539823$ or -8.120 or -8.119

Seven hours after the store opens, the rate that the customers remove bananas from the table is decreasing by $8.120 \frac{\text{pounds}}{\text{hr}^2}$.

(c)

$f(5) \approx 13.796 \frac{\text{pounds}}{\text{hr}}$ removed $g(5) \approx 11.532 \frac{\text{pounds}}{\text{hr}}$ added

The number of pounds on the table at $t = 5$ is **decreasing** since $f(5) > g(5)$.
or consider:

Amount of bananas at any time, $A(t) = 50 - \int_0^t f(x) dx + \int_3^t g(x) dx$

$A'(t) = -f(t) + g(t)$

$A'(5) = -f(5) + g(5) \approx -13.796 + 11.532 < 0$

Hence the amount of bananas on the table is decreasing at $t = 5$.

(d)

Pounds of bananas on table at $t = 8$ is the pounds at opening – pounds removed + pounds added

$50 - \int_0^8 f(t) dt + \int_3^8 g(t) dt \approx 23.34739574$ pounds or 23.347 pounds